Numbered list of outputs referenced in the Impact Report for the following project:

# Enhancing students' proof competencies in secondary mathematics classrooms (RES-000-22-2536-A)

Andreas J. Stylianides University of Cambridge

#### **PUBLICATIONS**

# Journal Articles:

- i. **Stylianides, A. J.**, & Al-Murani, T. (2010). Can a proof and a counterexample coexist? Students' conceptions about the relationship between proof and refutation. *Research in Mathematics Education*, 12(1), 21-36.
- ii. **Stylianides, A. J.** (2009). Breaking the equation "empirical argument = proof". *Mathematics Teaching*, 213, 9-14.

<u>Note</u>: The NRICH project republished the article at its popular open-access website having obtained permission from the Association of Teachers of Mathematics, which publishes Mathematics Teaching. The republished article at the NRICH website (<a href="http://nrich.maths.org/public/viewer.php?obj\_id=6664">http://nrich.maths.org/public/viewer.php?obj\_id=6664</a>) is accompanied with excerpts from an interview given by Andreas Stylianides to the NRICH director, Dr Jenny Piggott, about ideas in the article (<a href="http://nrich.maths.org/public/viewer.php?obj\_id=6664&part=note">http://nrich.maths.org/public/viewer.php?obj\_id=6664&part=note</a>).

# Invited Article in Conference Proceedings (Plenary Lecture):

iii. **Stylianides, A. J.** (2009). Towards a more comprehensive "knowledge package" for teaching proof. In J. H. Meyer & A. van Biljon (Eds.), *Proceedings of the 15th Annual Congress of the Association for Mathematics Education of South Africa (AMESA)* (Vol. 1, pp. 242-263). University of the Free State, Bloemfontein, South Africa.

# Conference Articles:

- iv. **Stylianides, A. J.**, & Stylianides, G. J. (2010). Toward the design of instructional interventions in the area of proof. In A. Gagatsis, T. Rowland, A. Panaoura, & A. Stylianides (Eds.), *Mathematics education research at the University of Cyprus and the University of Cambridge: A symposium* (pp. 203-218). Nicosia, Cyprus: School of Social Sciences and Sciences of Education, University of Cyprus.
- v. **Stylianides, A. J.**, & Al-Murani, T. (2009). "Can a proof and a counterexample coexist?" A study of students' conceptions about proof. In, *Proceedings of the 6th Congress of the European Society for Research in Mathematics Education* (pp. 311-321). France, Lyon.
- vi. **Stylianides, A. J.**, & Stylianides, G. J. (2008). "Cognitive conflict" as a mechanism for supporting developmental progressions in students' knowledge about proof. In, *Online Proceedings of the 11th International Congress on Mathematical Education (ICME)*, under Topic Study Group 18 (http://tsg.icme11.org/tsg/show/19). Monterrey, Mexico.

# Chapters in an Edited Volume:

- vii. **Stylianides, A. J.**, & Stylianides, G. J. (in press). Mathematical reasoning and proof (Part 1 of 2: student edition). In P. Palhares (Editor and translator of the chapter from English to Portuguese), *Complements of mathematics for primary teachers*. Lidel.
- viii. **Stylianides, A. J.**, & Stylianides, G. J. (in press). Mathematical reasoning and proof (Part 2 of 2: instructor's guidance). In P. Palhares (Editor and translator of the chapter from English to Portuguese), *Complements of mathematics for primary teachers*. Lidel.

#### INVITED RESEARCH LECTURES/PRESENTATIONS

- ix. (2011, April). (w/ G. J. Stylianides). Supporting progressions in students' justification schemes: results from two design experiments in the domain of proof. *Invited research seminar at the joint seminar series of the University of California at San Diego and San Diego State University*, San Diego State University, San Diego, California, USA.
- x. (2011, January). (w/ G. J. Stylianides). Engineering cognitive conflicts that support conceptual change: results from two design experiments in the domain of proof. *Invited research seminar at the Midlands Mathematics Education Seminar Series (participating institutions: the Universities of Birmingham, Leicester, Loughborough, Nottingham, and Warwick)*, University of Loughborough, Loughborough, UK.
- xi. (2010, June). Classroom-based design experiments in educational research: a study on the "cognitive conflict" approach to mathematics teaching. *Invited research presentation at the e-Learning Research Group Seminar Series*, Department of Education, University of Oxford, Oxford, UK.
- xii. (2009, July). Towards a more comprehensive "knowledge package" for teaching proof. *Invited plenary lecture at the 15th Annual Congress of the Association for Mathematics Education of South Africa (AMESA)*, University of the Free State, Bloemfontein, South Africa.
- xiii. (2009, June). The "cognitive conflict" approach to mathematics teaching: The case of proof. *Invited research presentation at the Tshwane University of Technology*, South Africa.

#### OTHER RESEARCH PRESENTATIONS

- xiv. (2009, November). (w/ E. Demosthenous). What might be involved in the development of a credible picture of students' understanding of proof? *Presentation at the Conference of the British Society for Research into Learning Mathematics (BSRLM)*, Loughborough University, Loughborough, UK.
- xv. (2009, March). Students' conceptions about the relationship between proof and refutation in mathematics. *Presentation at the 2009 Annual CamERA Research Conference*, University of Cambridge, Cambridge, UK.
- xvi. (2009, January). (w/ G. J. Stylianides). The "cognitive conflict" approach to mathematics teaching. *Presentation at the Mathematics Education Colloquium Series*, University of Cambridge, Cambridge, UK.

### SEMINARS/WORKSHOPS

- xvii. (2010, June). Enhancing students' proof competencies in secondary mathematics classrooms. Workshop to about 30 secondary mathematics mentor teachers who work with secondary mathematics teacher trainees enrolled in the Secondary Mathematics PGCE Course, University of Cambridge Faculty of Education, Cambridge, UK.
- xviii. (2010, May). (w/ S. Hennessy). Design-based research. Workshop to about 30 MEd students enrolled in the Research Methods Course, University of Cambridge Faculty of Education, Cambridge, UK.
- xix. (2010, April). (w/ K. Russell). Introducing secondary school students to the notion of proof in mathematics. Workshop to about 40 researchers, teachers, teacher educators, curriculum developers, and policy makers at the 7th British Congress of Mathematics Education (BCME), University of Manchester, Manchester, UK.
- xx. (2010 & 2009, February). Design experiments in educational research. *Workshops to a total of about 90 MPhil students enrolled in the Core Research Training Course*, University of Cambridge Faculty of Education, Cambridge, UK.
- xxi. (2010, January). The teaching and learning of proof in secondary school mathematics. Workshop to about 30 secondary mathematics teacher trainees enrolled in the Secondary Mathematics PGCE Course, University of Cambridge Faculty of Education, Cambridge, UK.

xxii. (2008, June). (w/ T. Al-Murani). Proof in secondary school mathematics. Workshop to about 25 secondary teachers, secondary teacher trainees, and researchers as part of the University of Oxford Mathematics Education Seminar Series, University of Oxford, Oxford, UK.